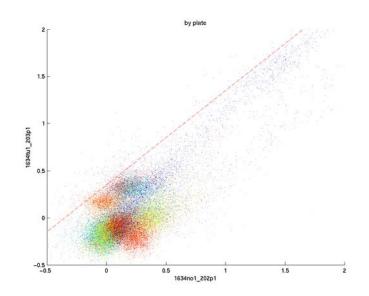
# Error models and normalization

Wolfgang Huber DKFZ Heidelberg



## Acknowledgements

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Sandrine Dudoit, Robert Gentleman, Rafael Irizarry and Yee Hwa Yang: Bioconductor short course, summer 2002

and many others

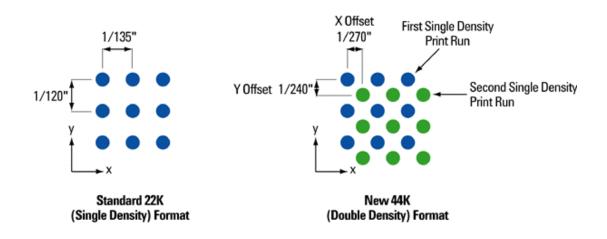
### A microarray slide (spotted) Slide: 25x75 mm 4x4, 8x4, or 12x 4 **Spot-to-spot:** ca. 150-350 μm sectors 17...38 rows and columns per sector ca. 4000...46000 probes/array -sector: corresponds to one print-tip

## Affymetrix oligonucleotide chips

| hgU133plus2.0                          |         |  |
|--|---------|--|
| Feature size                           | 11µm    |  |
| No. probes                             | 600,000 |  |
| No. probe pairs per<br>target sequence | 11      |  |
| Oligonucleotide<br>length              | 25      |  |

## Agilent oligonucleotide chips

| whole human genome kit (5/2004) |        |  |
|---------------------------------|--------|--|
| Feature size                    | ≈100µm |  |
| No. probes                      | 44,000 |  |
| Oligonucleotide length          | 60     |  |



### Terminology

- sample: RNA (cDNA) hybridized to the array, aka target, mobile substrate.
- probe: DNA spotted on the array, aka spot, immobile substrate.
- sector: rectangular matrix of spots printed using the same print-tip (or pin), aka print-tip-group plate: set of 384 (768) spots printed with DNA from the same microtitre plate of clones slide, array
- channel: data from one color (Cy3 = cyanine 3 =
  green, Cy5 = cyanine 5 = red).
- batch: collection of microarrays with the same probe layout.

scanner signal

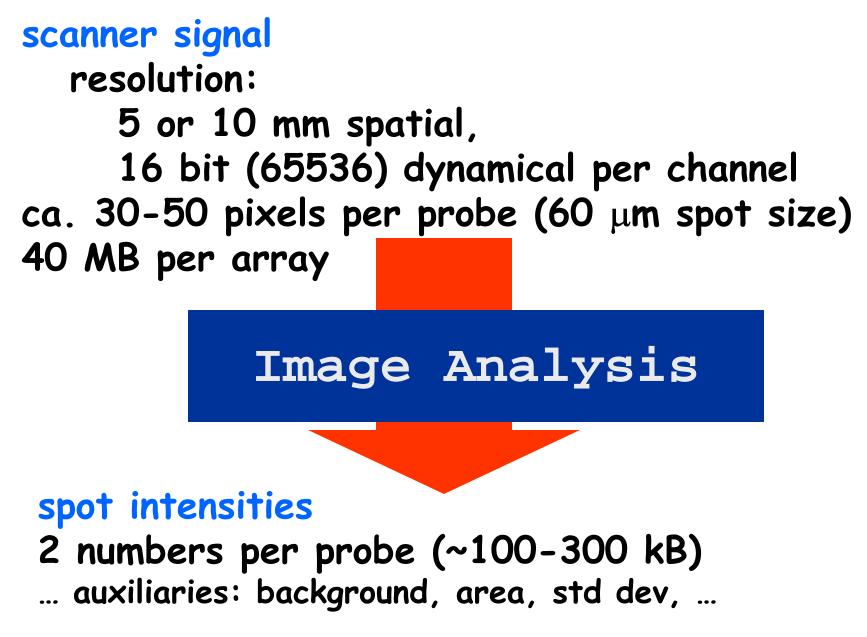
resolution:

5 or 10 mm spatial,

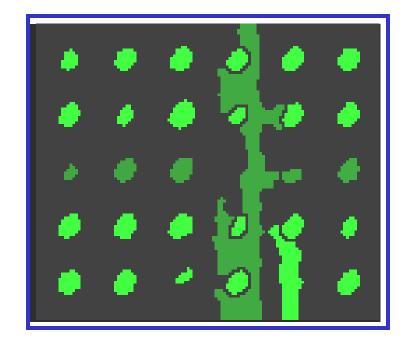
16 bit (65536) dynamical per channel

ca. 30-50 pixels per probe (60  $\mu\text{m}$  spot size) 40 MB per array

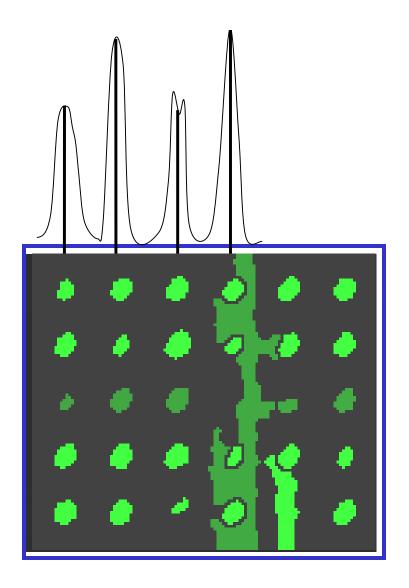
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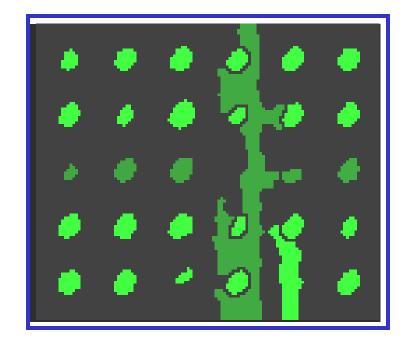
1. Addressing. Estimate location of spot centers.



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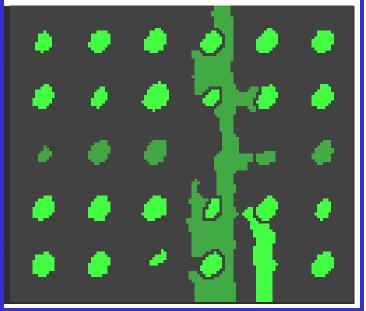


1. Addressing. Estimate location of spot centers.



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2. Segmentation. Classify pixels as foreground (signal) or background.

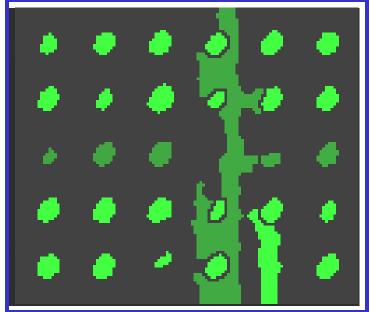


1. Addressing. Estimate location of spot centers.

2. Segmentation. Classify pixels as foreground (signal) or background.

3. Information extraction. For each spot on the array and each dye

- foreground intensities;
- background intensities;
- quality measures.



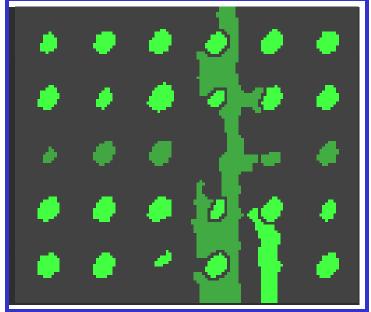
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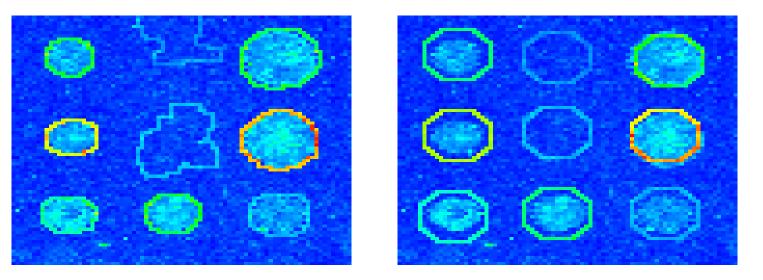
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## Segmentation

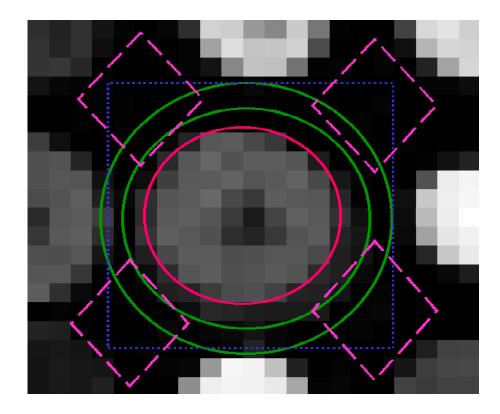


fixed circle segmentation

adaptive segmentation seeded region growing

### Spots may vary in size and shape.

## Local background



----- GenePix ----- QuantArray ----- ScanAlyze

Image is probed with a window (aka structuring element), eg, a square with side length about twice the spot-to-spot distance.

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 $\Rightarrow$  Image of the estimated background

### What is (local) background?

### usual assumption:

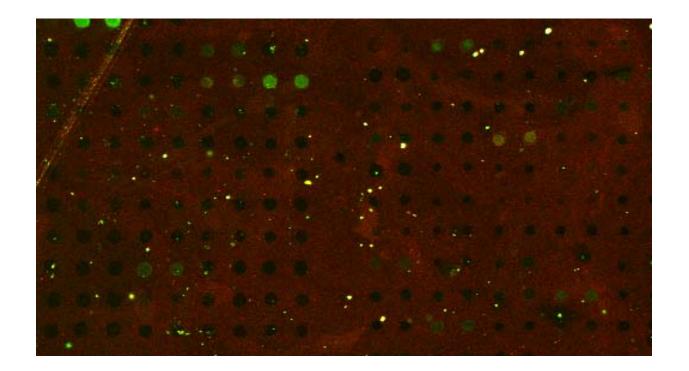
## total brightness = background brightness (adjacent to spot)

+ brightness from labeled sample cDNA

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## total brightness = background brightness (adjacent to spot) the brightness from labeled sample cDNA



## Affymetrix files

### Main software from Affymetrix:

MAS - MicroArray Suite.

- DAT file: Image file, ~10^7 pixels, ~50 MB.
- CEL file: probe intensities, ~500,000 numbers

CDF file: Chip Description File. Describes which probes go in which probe sets (genes, gene fragments, ESTs).

DAT image files  $\rightarrow$  CEL files

Each probe cell: 10x10 pixels.

Gridding: estimate location of probe cell centers.

Signal:

- Remove outer 36 pixels -> 8x8 pixels.
- The probe cell signal, PM or MM, is the 75<sup>th</sup> percentile of the 8x8 pixel values.
- Background: Average of the lowest 2% probe cells is taken as the background value and subtracted.

Compute also quality values.

## Quality measures

### Spot quality

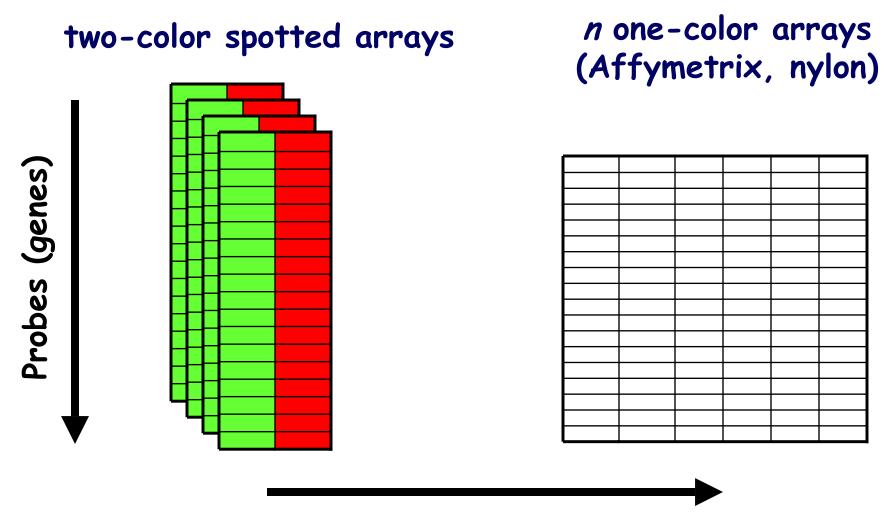
- Brightness: foreground/background ratio
- Uniformity: variation in pixel intensities and ratios of intensities within a spot
- Morphology: area, perimeter, circularity.

### Slide quality

- Percentage of spots with no signal
- Range of intensities
- Distribution of spot signal area, etc.

## How to use quality measures in subsequent analyses?

### spot intensity data

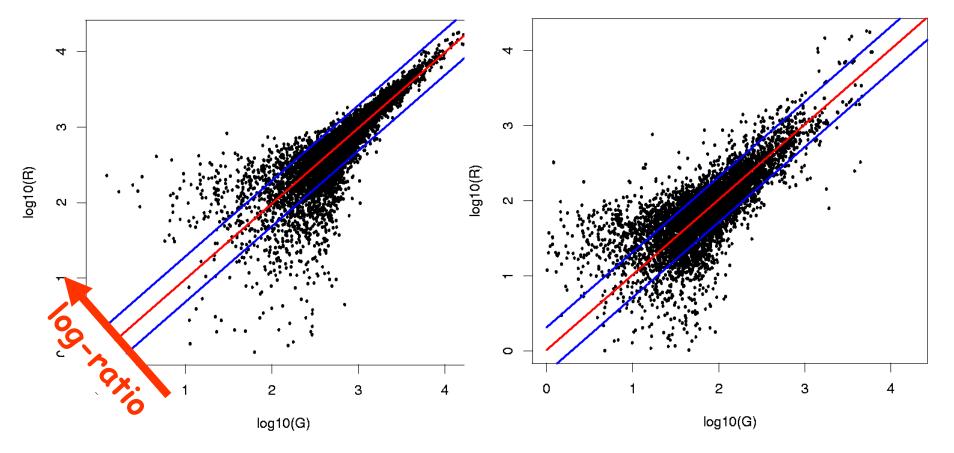


conditions (samples)

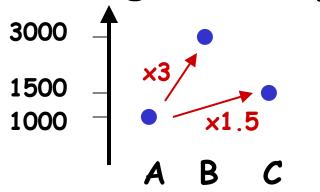
### Which genes are differentially transcribed?

#### same-same

#### tumor-normal



## Fold changes are useful to describe continuous changes in expression



## But what if the gene is "off" (below detection limit) in one condition?

The idea of the log-ratio (base 2)

0: no change

+1: up by factor of  $2^1 = 2$ 

+2: up by factor of  $2^2 = 4$ 

-1: down by factor of  $2^{-1} = 1/2$ 

-2: down by factor of  $2^{-2} = \frac{1}{4}$ 

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A unit for measuring changes in expression: assumes that a change from 1000 to 2000 units has a similar biological meaning to one from 5000 to 10000.

#### What about a change from 0 to 500?

- conceptually
- noise, measurement precision

### Raw data are not mRNA concentrations

o tissue contamination

**o** RNA degradation o amplification efficiency o reverse transcription efficiency o hybridization efficiency and specificity

o clone
identification and
mapping
o PCR yield,
contamination
o spotting
efficiency
o DNA-support
binding

o other array manufacturingrelated issues o image segmentation

signal
quantification
'background'
correction

| Raw   | data are not mRNA concentrations  |
|---|---|
| o tissue<br>cor   | o clone o image   |
| o R<br>deg<br>o a<br>eff<br>o r<br>tra<br>eff<br>o h<br>eff | The problem is less that these<br>steps are 'not perfect'; it is<br>that they may vary from array<br>to array, experiment to<br>experiment. |
| specifici   | ty related issues   |

### Sources of variation

- amount of RNA in the biopsy efficiencies of
- -RNA extraction
- -reverse transcription
- -labeling
- -photodetection

PCR yield DNA quality spotting efficiency, spot size cross-/unspecific hybridization stray signal

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## Systematic

similar effect on many measurements
corrections can be estimated from data

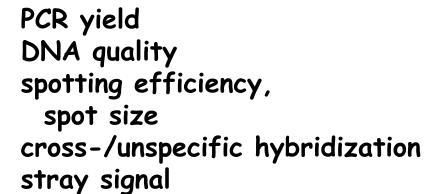
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Calibration



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PCR yield DNA quality spotting efficiency, spot size cross-/unspecific hybridization stray signal

## Stochastic

too random to be explicitely accounted for
"noise"

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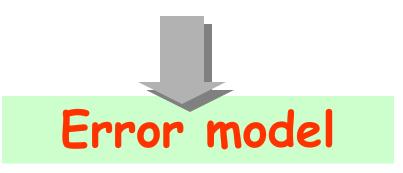
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## Error models

## **Definition:**

description of the possible outcomes of a measurement

## Depends on:

-true value of the measured quantity (abundances of specific molecules in biological sample)

### -measurement apparatus

(cascade of biochemical reactions, optical detection system with laser scanner or CCD camera)

## Error models

## Purpose:

- 1. statistical inference (appropriate parametric methods have better power)
- 2. summarization (summary statistic instead of full empirical distribution)
- 3. quality control

# y = f(x,u)

- y measurement
- f measurement apparatus
- x true underlying quantity
- u further factors that can influence the measurement ("environment")

$$y = f(x, u)$$

$$y = f(0, u) + f'(0, u) \cdot x + O(x^2)$$

$$f(0,u) \approx f(0,\overline{u}) + \sum_{i} \frac{\partial f(0,u)}{\partial u_{i}} (u_{i} - \overline{u_{i}})$$

$$f'(0,u) \approx f'(0,\overline{u}) + \sum_{i} \frac{\partial f'(0,u)}{\partial u_{i}} (u_{i} - \overline{u_{i}})$$

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approximation of  
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 $y = a + \varepsilon + b \cdot x \cdot (1 + \eta)$ 

model environment fluctuations as noise

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fluctuations as noise

y = f(x, u)generic observation eqn. (x=true value, u=environment)  $y = f(0, u) + f'(0, u) \cdot x + O(x^2)$ first order approximation of x-dependence of f  $f(0,u) \approx f(0,\overline{u}) + \sum \frac{\partial f(0,u)}{\partial u} (u_i - \overline{u_i})$ first order approximation of u-dependence of f  $f'(0,u) \approx f'(0,\overline{u}) + \sum_{i} \frac{\partial f'(0,u)}{\partial u_{i}} (u_{i} - \overline{u_{i}})$ first order approximation of u-dependence of f' model environment  $y = a + \varepsilon + b \cdot x \cdot (1 + \eta)$ fluctuations as noise

## Parameterization

$$y = a + \varepsilon + b \cdot x \cdot (1 + \eta)$$
$$y = a + \varepsilon + b \cdot x \cdot e^{\eta}$$

two practically equivalent forms (η<<1)

| a systematic<br>background           | same for all<br>probes per array x<br>color | array x color x<br>print-tip group |
|--------------------------------------|---|------------------------------------|
| ε random<br>background               | iid in whole<br>experiment                  | iid per array                      |
| b systematic gain<br>factor          | array x color                               | array x color x<br>print-tip group |
| η <b>random gain</b><br>fluctuations | iid in whole<br>experiment                  | iid per array                      |

## Important issues for model fitting

### Parameterization variance vs bias

## "Heteroskedasticity" (unequal variances) ⇒ weighted regression or variance stabilizing transformation

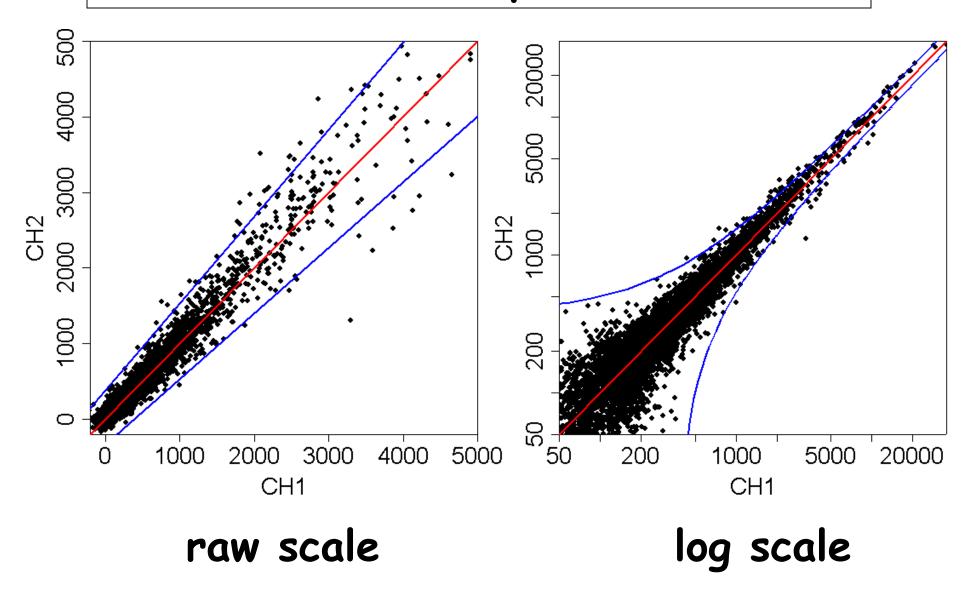
### Outliers

 $\Rightarrow$  use a robust method

### Algorithm

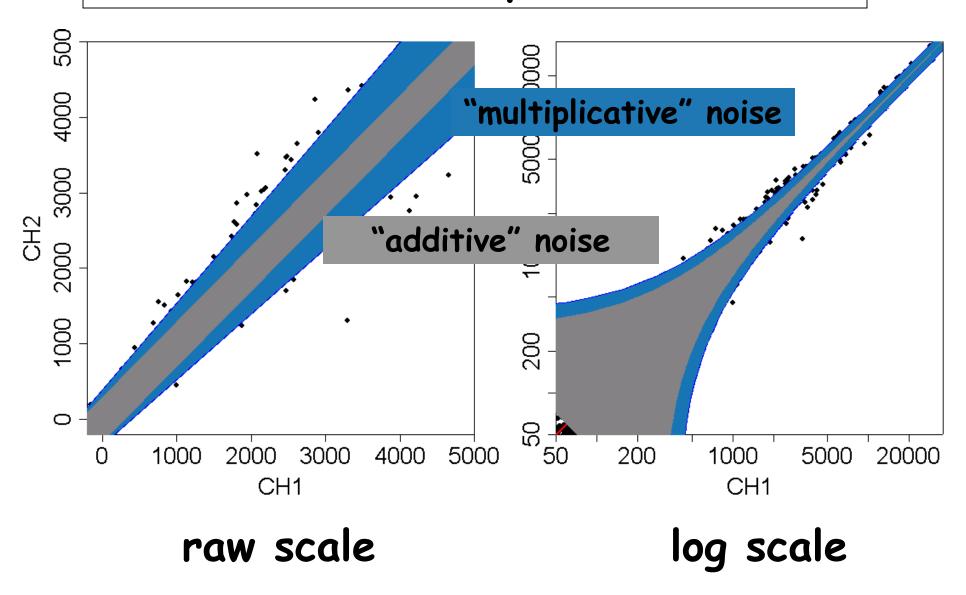
If likelihood is not quadratic, need non-linear optimization. Local minima / concavity of likelihood?

## The two-component model



B. Durbin, D. Rocke, JCB 2001

### The two-component model



B. Durbin, D. Rocke, JCB 2001

## Nesting

$$y = a + \varepsilon + b \cdot x \cdot (1 + \eta)$$

$$x = a' + \varepsilon' + b' \cdot z \cdot (1 + \eta')$$

$$\downarrow$$

$$a = a' + \varepsilon' + b' \cdot z \cdot (1 + \eta')$$

$$\downarrow$$

$$a = a' + \varepsilon' + b' \cdot z \cdot (1 + \eta')$$

$$\downarrow$$

$$b = a = a' + \varepsilon' + b' \cdot z \cdot (1 + \eta')$$

$$\downarrow$$

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$$\downarrow$$

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$$\downarrow$$

$$b = a = a' + \varepsilon' + b' \cdot z \cdot (1 + \eta')$$

$$c = a = a' + \varepsilon' + b' \cdot z \cdot (1 + \eta')$$

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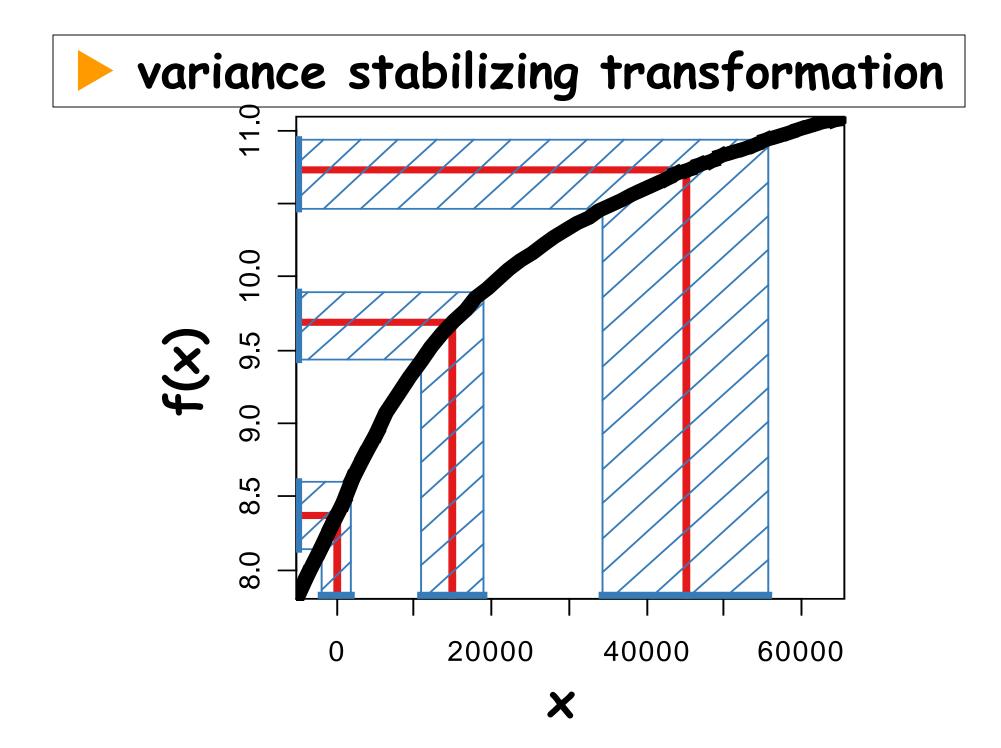
$$c = a = a' + \varepsilon' + b' \cdot z \cdot (1 + \eta')$$

 $y \approx a'' + \varepsilon'' + b'' \cdot z \cdot (1 + \eta'')$  overall

# variance stabilization

 $X_{\mu}$  a family of random variables with  $EX_{\mu}=u$ ,  $VarX_{\mu}=v(u)$ . Define  $f(x) = \int \frac{1}{\sqrt{v(u)}} du$  $\Rightarrow$  var  $f(X_{\mu}) \approx$  independent of u

derivation: linear approximation



## variance stabilizing transformations

$$f(x) = \int_{-\infty}^{x} \frac{1}{\sqrt{v(u)}} du$$

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$$f(x) = \int_{-\infty}^{x} \frac{1}{\sqrt{v(u)}} du$$

1.) constant variance

$$v(u) = const \Rightarrow f \propto u$$

## >variance stabilizing transformations

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- 1.) constant variance  $v(u) = const \Rightarrow f \propto u$
- 2.) const. coeff. of variation  $v(u) \propto u^2 \implies f \propto \log u$

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3.) offset  $v(u) \propto (u + u_0)^2 \Rightarrow f \propto \log(u + u_0)$ 

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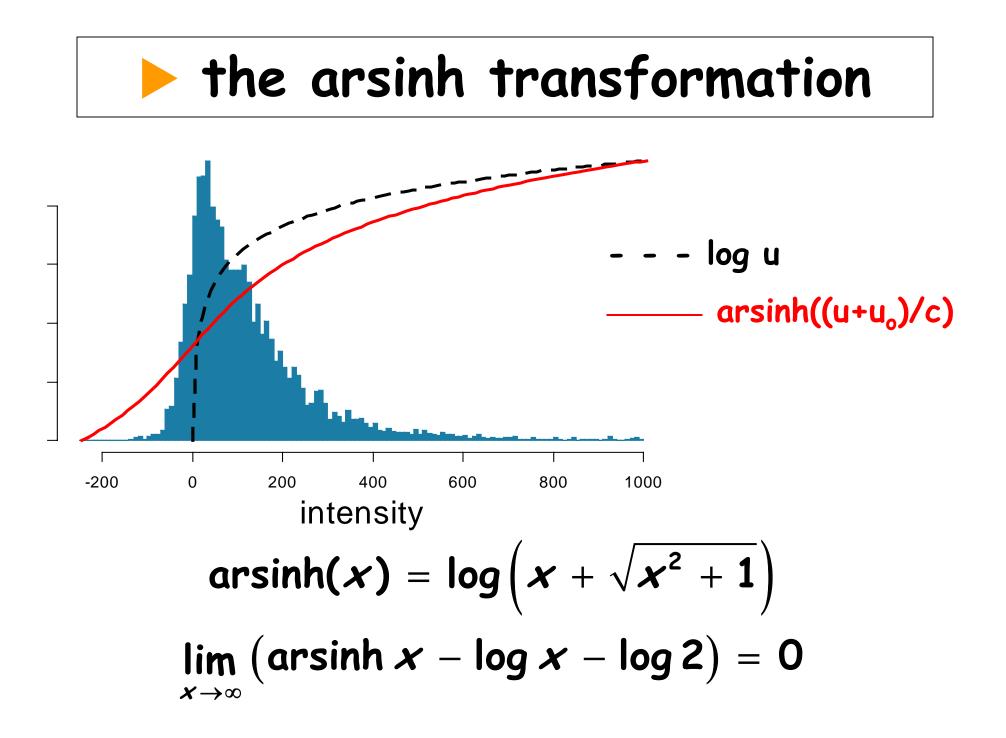
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3.) offset  $v(u) \propto (u + u_0)^2 \Rightarrow f \propto \log(u + u_0)$ 

4.) microarray

$$v(u) \propto (u + u_0)^2 + s^2 \Rightarrow f \propto \operatorname{arsinh} \frac{u + u_0}{s}$$



the transformed model

 $\frac{\mathbf{y}_{ki} - \mathbf{a}_{si}}{\mathbf{b}_{si}} = \mu_k + \varepsilon_{ki}$ 

# $\varepsilon_{ki}: N(0, c^2)$

- i: arrays
- k: probes
- s: probe strata (e.g. print-tip, region)



 $pll(a,b) = \sup ll(a,b,c,\mu)$ С,μ

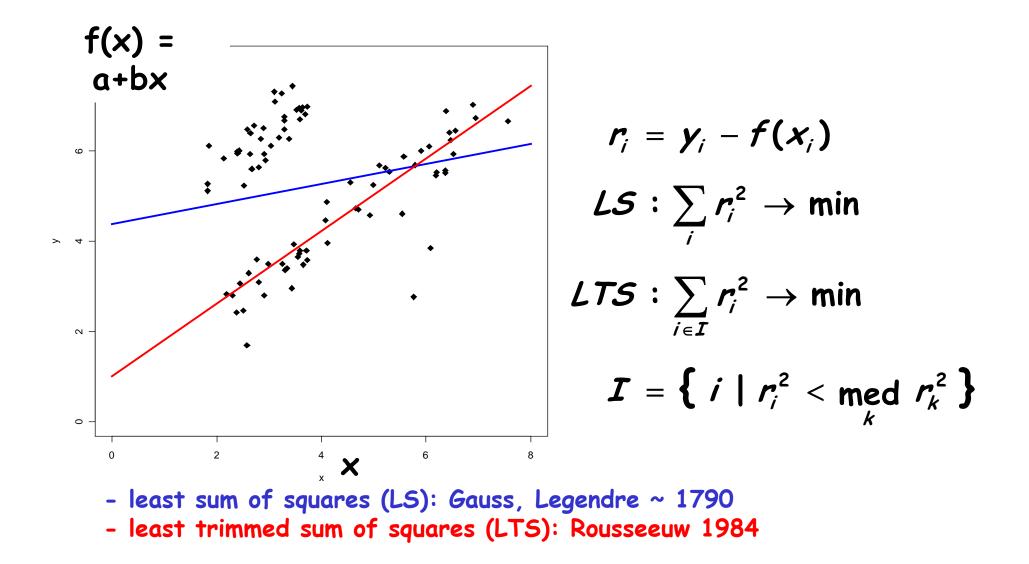


$$pll(a,b) = \sup_{c,\mu} ll(a,b,c,\mu)$$

#### Here:

$$pll(a_1, b_1, \dots, a_d, b_d) = \\ = -nd\log\hat{\sigma} + \sum_{k=1}^n \sum_{i=1}^d \log h'_i(y_{ki}) \\ = -\frac{nd}{2}\log\left(\sum_{k=1}^n \sum_{i=1}^d (h_i(y_{ki}) - \hat{\mu}_k)^2\right) + \sum_{k=1}^n \sum_{i=1}^d \log h'_i(y_{ki})$$

## Least trimmed sum of squares regression

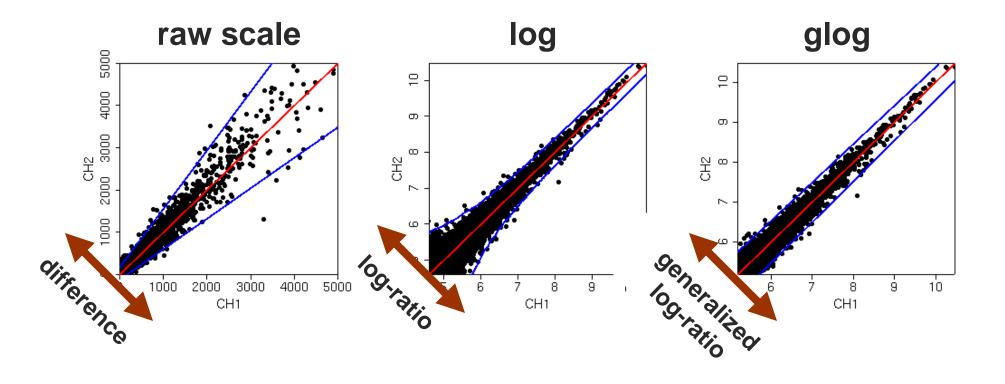


#### evaluation: effects of different data transformations b) ∆log(y) a) ∆y N -500 -1000 n c) $\Delta h(y)$ red-green difference Υ.

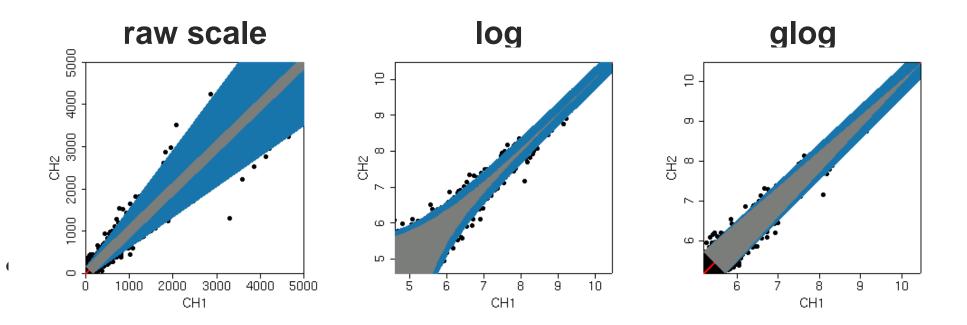
rank(average)

n

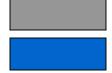








#### variance:



constant part proportional part

# Motivation for the generalized log-ratio

# $z_1$ , $z_2 \sim additive-multiplicative error model Search function h that fulfills$

(i) 
$$h(z_1, z_2) = -h(z_2, z_1)$$
  
(ii)  $Var(h(z_1, z_2)) \approx const.$ 

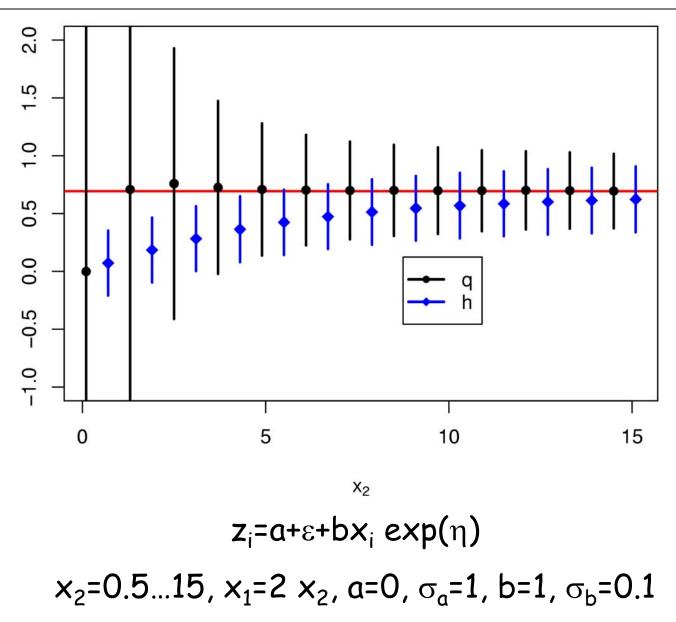
$$\Rightarrow h(z_1, z_2) = asinh(\frac{z_1 - a}{b}) - asinh(\frac{z_s - a}{b})$$

# Properties of the generalized log-ratio

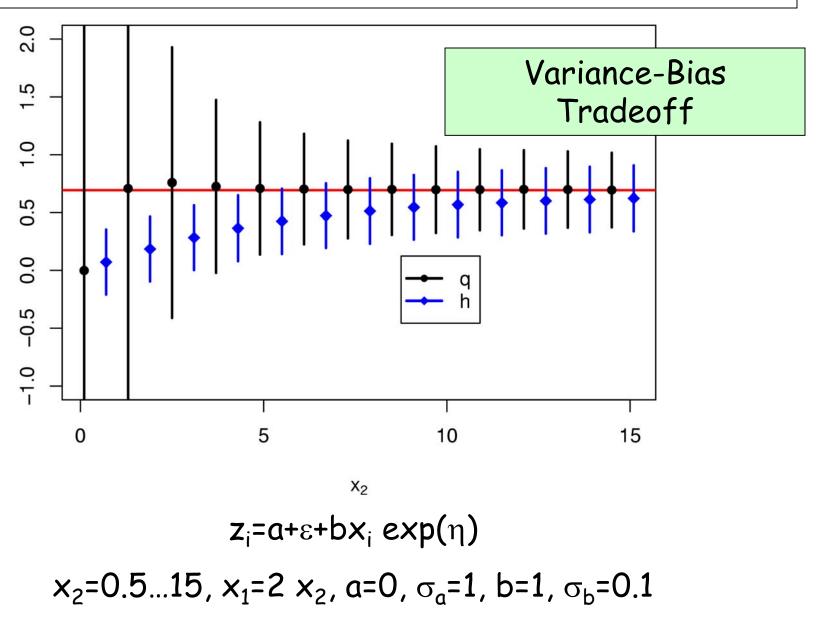
$$h(z_1, z_2) = asinh(\frac{z_1 - a}{b}) - asinh(\frac{z_2 - a}{b})$$
$$q(z_1, z_2) = \log(z_1 - a) - \log(z_2 - a)$$

(i) for  $z_1$ ,  $z_2 > a$ , h and q are the same (ii)  $|h(z_1, z_2)| \le |q(z_1, z_2)|$ (iii)  $exp(h(z_1, z_2))$  is a shrinkage estimator for fold-change

## Properties of the generalized log-ratio



# Properties of the generalized log-ratio



# Summary

log-ratio  $\frac{\log \frac{Y_{k1} - a_1}{b_1} - \log \frac{Y_{k2} - a_2}{b_2}}{b_2}$ 

'generalized' log-ratio

$$\frac{Y_{k1} - a_1}{b_1} - \operatorname{arsinh} \frac{Y_{k2} - a_2}{b_2}$$

o advantages of variance-stabilizing data-transformation: generally better applicability of statistical methods (hypothesis testing, ANOVA, clustering, classification...)

o R package vsn

## "Single color normalization"

n red-green arrays ( $R_1$ ,  $G_1$ ,  $R_2$ ,  $G_2$ ,...  $R_n$ ,  $G_n$ )

#### within/between slides

for (i=1:n) calculate  $M_i = \log(R_i/G_i)$ ,  $A_i = \frac{1}{2} \log(R_i^*G_i)$ normalize  $M_i$  vs  $A_i$ normalize  $M_1...M_n$ 

#### all at once

normalize the matrix of (R, G) then calculate log-ratios or any other contrast you like

# How to compare and assess different 'preprocessing' methods

Normalization = correction for systematic experimental biases + provision of an expression value that can be used subsequently for testing, clustering, classification, modelling.

Quality trade-off: the better the measurements, the less normalization

Variance-Bias trade-off: how do you weigh measurements that have low signal-noise ratio?

How to compare and assess different 'normalization' methods?

#### Normalization :=

 correction for systematic experimental biases
 provision of expression values that can subsequently be used for testing, clustering, classification, modelling...
 provision of a measure of measurement uncertainty

Quality trade-off: the better the measurements, the less need for normalization. Need for "too much" normalization relates to a quality problem.

Variance-Bias trade-off: how do you weigh measurements that have low signal-noise ratio?

- just use anyway
- ignore
- shrink

## How to compare and assess different 'normalization' methods?

#### Aesthetic criteria

Logarithm is more beautiful than arsinh

#### Practical critera

It takes forever to run vsn. Referees will only accept my paper if it uses the original MAS5.

#### Silly criteria

The best method is that that makes all my scatterplots look like straight, slim cigars

#### Physical criteria

Normalization calculations should be based on physical/chemical model

#### Economical/political criteria

Life would be so much easier if everybody were just using the same method, who cares which one

### How to compare and assess different 'normalization' methods?

Comparison against a ground truth But you have millions of numbers – need to choose the metric that measures deviation from truth. FN/FP: do you find all the differentially expressed genes, and do you not find non-d.e. genes? qualitative/quantitative: how well do you estimate abundance, fold-change?

## Spike-In and Dilution series

... great, but how representative are they of other data?

# Implicitely, from resampling the actual experiment of interest

... but isn't that too much like Munchhausen?

evaluation: a benchmark for Affymetrix genechip expression measures

o Data:

Spike-in series: from Affymetrix 59 x HGU95A, 16 genes, 14 concentrations, complex background Dilution series: from GeneLogic 60 x HGU95Av2, liver & CNS cRNA in different proportions and amounts

#### o Benchmark:

15 quality measures regarding

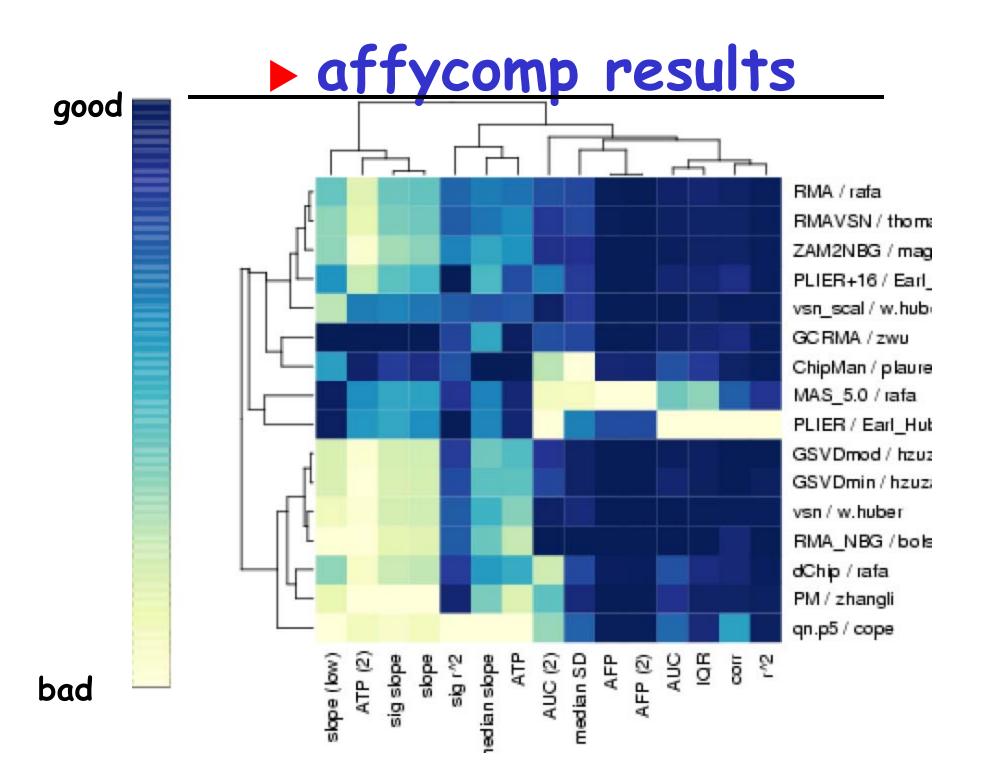
-reproducibility

- -sensitivity
- -specificity

Put together by Rafael Irizarry (Johns Hopkins) http://affycomp.biostat.jhsph.edu evaluation: a benchmark for Affymetrix genechip expression measures

• Package affycomp (on Bioconductor)

o Online competition, accepts contributions via webserver







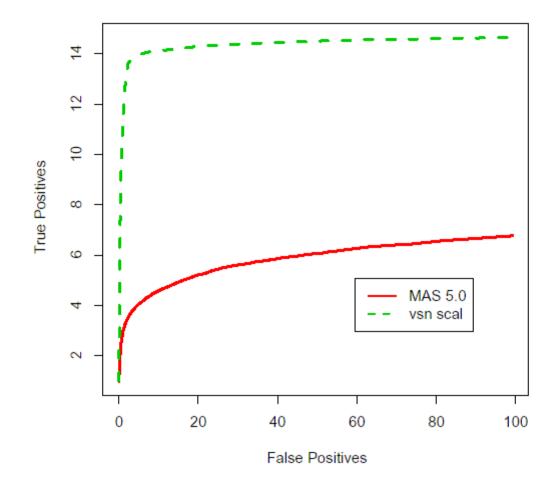


Figure 5a): A typical identification rule for differential expression filters genes with fold change exceeding a given threshold. This figure shows average ROC curves which offer a graphical representation of both specificity and sensitivity for such a detection rule. Average ROC curves based on comparisons with nominal fold changes ranging from 2 to 4096. b) As a) but with nominal fold changes equal to 2.

Affymetrix preprocessing involves (1) PM, MM-synthesis (2) calibration, transformation (3) probe set summarization

## 'vsn-scal' used

- (1) ignore MM
- (2) vsn
- (3) medianpolish (as in RMA, similar to dChip)

## This can be improved

(1) use MM! (but just not simply PM-MM)(2) stratify by physical probe properties

# Resampling method: sensitivity / specificity in detecting differential abundance

o Data: paired tumor/normal tissue from 19 kidney cancers, in color flip duplicates on 38 cDNA slides à 4000 genes.

o 6 different strategies for normalization and quantification of differential abundance

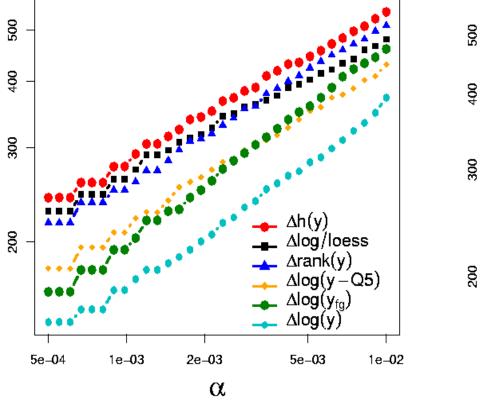
Calculate for each gene & each method:
 *t*-statistics, permutation-p

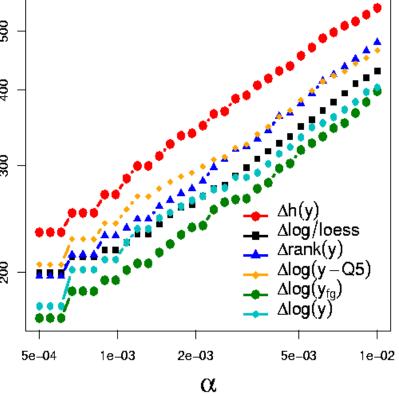
o For threshold  $\alpha$ , compare the number of genes the different methods find,  $\#\{p_i \mid p_i \le \alpha\}$ 

## sensitivity vs specificity

one-sided test for up

#### one-sided test for down





### Summary

Measuring microarray data is a complex chain of biochemical reactions and physical measurements.

Systematic and stochastic errors

Calibration and error models

Parameter estimation

Getting preprocessing right is prerequisite for getting reasonable results in the end

Improving preprocessing is just like any other technology improvement

How to choose from the plethora of methods?

## What's next

Exercises on data import, diagnostic plots, quality criteria, comparing normalization methods

Lecture on **quality control**, probe set summaries, hybridization physics

Thank you